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To me style is just the outside of content, and content the inside of style, like the outside and the inside of the human body both go together, they can't be separated.

Jean-Luc Godard

